

1. The 10kg mass is in static equilibrium. Find the tensions in the two segments of rope.

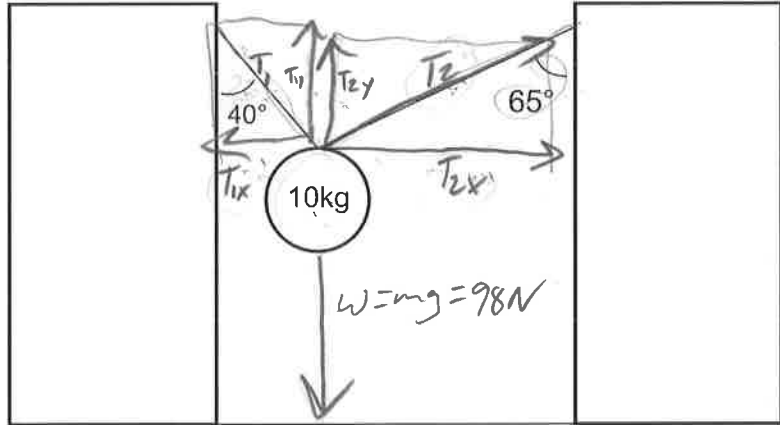
$$\sum F_x = 0 = T_{2x} - T_{1x}$$

$$T_{2x} = T_{1x}$$

$$\sin 65^\circ T_2 = \sin 40^\circ T_1$$

$$0.906 T_2 = 0.643 T_1$$

$$T_2 = 0.71 T_1$$



$$\sum F_y = 0 = T_{1y} + T_{2y} - 98N$$

$$0 = \cos 40^\circ T_1 + \cos 65^\circ T_2 - 98N$$

$$0 = 0.766 T_1 + 0.423 T_2 - 98N = 0.766 T_1 + 0.423 (0.71 T_1) - 98N$$

$$0 = 0.766 T_1 + 0.3 T_1 - 98N$$

$$T_1 = 91.5N$$

$$T_2 = 0.71 T_1 = 65N$$

2. Find the acceleration of the masses and the tension in the string.

$$a = 0 \text{ m/s}^2$$

$$T = 49N$$

$$W_{\perp} = \cos 40^\circ (58.8N) = 45N$$

$$W_{\parallel} = \sin 40^\circ (58.8N) = 37.8N$$

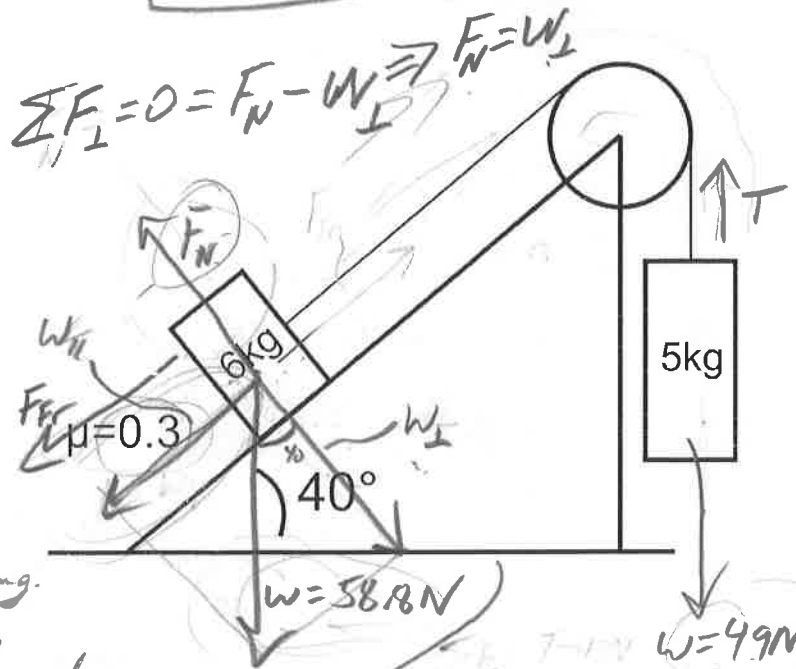
$$\sum F_{\parallel} = 49N - W_{\parallel} - F_f$$

$$\sum F_{\parallel} = 49N - 37.8N - \mu F_N$$

$$\sum F_{\parallel} = 11N - 0.3(45N)$$

$$\sum F_{\parallel} = 11N - 13.5N$$

Friction too strong.  
Adjusts to 11N, so  
no acceleration and  
 $\sum F_{\parallel} = 0$



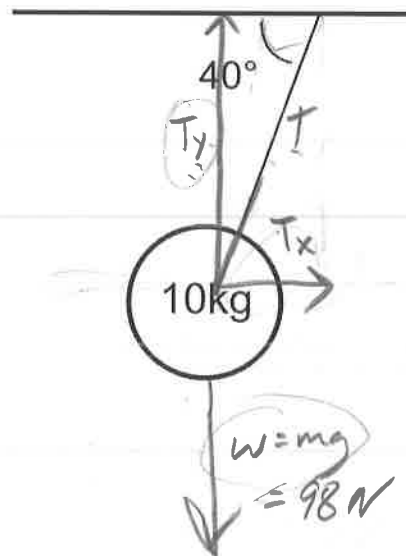
$$\sum F_{\perp} = 0 = F_N - W_{\perp} \Rightarrow F_N = W_{\perp}$$

$$\sum F_{5kg} = T - 49N = ma = 0$$

$$T = 49N$$

3.44N  
0.3m/s^2  
a = 0 m/s^2

3. The mass is suspended from the ceiling of a moving vehicle. The angle shown is constant. Find the acceleration of the mass and the tension in the string.



$$a = \underline{11.7 \text{ m/s}^2}$$

$$T = \underline{152 \text{ N}}$$

$$T_y = 98 \text{ N}$$

$$\frac{T_x}{T} = \cos 40^\circ$$

$$\frac{T_y}{T} = \sin 40^\circ$$

$$T_x = \cos 40^\circ T$$

$$T_y = \sin 40^\circ T$$

$$T_x = \cos 40^\circ (152 \text{ N})$$

$$98 \text{ N} = \sin 40^\circ T$$

$$T_x = \underline{117 \text{ N}}$$

$$\underline{152 \text{ N} = T}$$

$$\Sigma F = \Sigma F_x = T_x = ma$$

$$117 \text{ N} = 10 \text{ kg}(a)$$

$$\underline{a = 11.7 \text{ m/s}^2}$$

4. Find the acceleration of the 8kg mass.

$$\Sigma F_y = 0 = F_y + F_N - W$$

$$0 = 19.3 \text{ N} + F_N - 78.4$$

$$\underline{F_N = 59.1 \text{ N}}$$

$$F_y = \sin 40^\circ (30 \text{ N}) = 19.3 \text{ N}$$

$$F_x = \cos 40^\circ (30 \text{ N}) = 23.0 \text{ N}$$

$$\Sigma F_x = F_x - F_{fr}$$

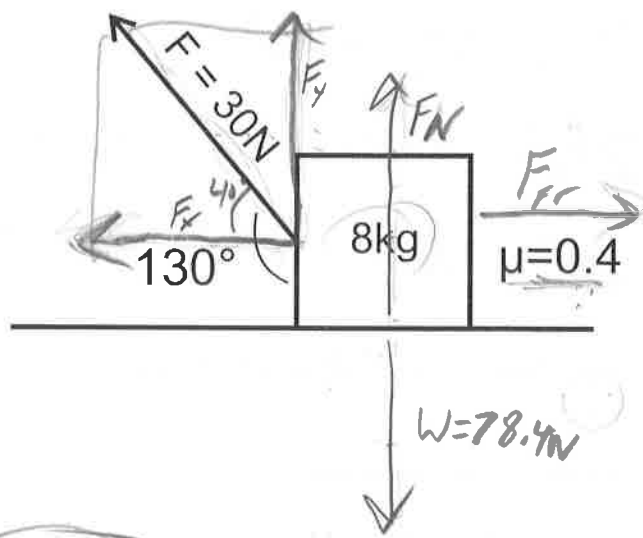
$$\Sigma F_x = 23.0 \text{ N} - \mu(F_N)$$

$$\Sigma F_x = 23.0 \text{ N} - 0.4(59.1 \text{ N})$$

$$\Sigma F_x = \underline{23.0 \text{ N} - 23.6 \text{ N}}$$

Friction stronger than pull.  
Friction adjusts to 23.6 N, so

$$\Sigma F = 0 \text{ and } \underline{a = 0 \text{ m/s}^2}$$



$$\underline{11.18 \text{ N leftward}}$$

$$\underline{1.4 \text{ m/s}^2 \text{ leftward}}$$