



$$1) F_{\text{spring}} = kx = 15 \text{ N/m} (0.25 \text{ m}) = 3.75 \text{ N}$$

$$2) \tau_{\text{rear}} = r_{\text{axle}} F_{\text{spring}} = 0.008 \text{ m} (3.75 \text{ N}) = 0.03 \text{ N}\cdot\text{m}$$

$$3) \tau_{\text{rear}} = r_{\text{wheel}} F_{\text{road}} \Rightarrow 0.03 \text{ N}\cdot\text{m} = 0.07 \text{ m} (F_{\text{road}})$$

$$F_{\text{road}} = 0.429 \text{ N}$$

$$4) PE_{\text{spring}} = \frac{1}{2} kx^2 = \frac{1}{2} (15 \text{ N/m}) (0.25 \text{ m})^2$$

$$= 0.469 \text{ J}$$

$$5) \text{Efficiency} = \frac{\text{Output}}{\text{Input}} \Rightarrow 0.5 = \frac{\text{Output}}{0.469 \text{ J}}$$

$$\text{Output} = 0.234 \text{ J}$$

$$b) KE = \frac{1}{2}mv^2 + \frac{1}{2}I_{\text{rear}}\omega_{\text{rear}}^2 + \frac{1}{2}I_{\text{front}}\omega_{\text{front}}^2$$

$$0 KE = \frac{1}{2}mv^2 + \left(\frac{1}{2}I_{\text{rear}}\frac{v^2}{r_{\text{rear}}^2} + \frac{1}{2}I_{\text{front}}\frac{v^2}{r_{\text{front}}^2}\right)$$

$$2KE = v^2 \left(m + \frac{I_{\text{rear}}}{r_{\text{rear}}^2} + \frac{I_{\text{front}}}{r_{\text{front}}^2} \right)$$

$$v = \sqrt{\frac{2KE}{\left(m + \frac{I_{\text{rear}}}{r_{\text{rear}}^2} + \frac{I_{\text{front}}}{r_{\text{front}}^2} \right)}}$$

$$v = \sqrt{\frac{2(0.234 \text{ J})}{0.15 \text{ kg} + \frac{0.0003 \text{ kg m}^2}{(0.07 \text{ m})^2} + \frac{0.0001 \text{ kg m}^2}{(0.05 \text{ m})^2}}}$$

$$v = \sqrt{\frac{0.468 \text{ J}}{0.15 \text{ kg} + 0.061 \text{ kg} + 0.04 \text{ kg}}}$$

$$v = \sqrt{\frac{4.95 \text{ m}^2}{52}} = 2.11 \text{ m/s}$$

$$7) \text{ Circumf. of rear axle} = 2\pi r = 2\pi(0.008\text{m}) = 0.0503\text{m}$$

0.0503m of string = 1 rotation

$$\left(\frac{0.1 \text{ rotation}}{0.0503 \text{ m string}} \right) (0.25 \text{ m string}) = 4.97 \text{ rotations of rear axle}$$

$$8) \text{ Circumf. of rear wheel} = 2\pi r = 2\pi(0.07\text{m}) = 0.44\text{m}$$

$$\frac{0.44\text{m of travel}}{0.1 \text{ rotation of rear wheel}} (4.97 \text{ rotations of rear wheel}) = 2.19\text{m}$$