

Name: Key

$$v = \omega (r)$$

$$\frac{m}{s} = \frac{rad}{s} \left(\frac{m}{rad} \right)$$

Notes - 10.1 Angular Acceleration

1. What is the definition of angular speed ω ? What are the units of ω ?

$$\omega = \frac{\Delta \theta}{\Delta t} \quad \text{units} \rightarrow \text{rad/s}$$

2. How are velocity and angular speed related?

$$v = \omega r$$

Where do the radians go?
Think of r as a ratio of meters per radian

3. What is the definition of angular acceleration α ? What are the units of α ?

$$\alpha = \frac{\Delta \omega}{\Delta t} \quad \text{units} \rightarrow \frac{rad}{s^2}$$

4. Suppose a teenager puts her bicycle on its back and starts the rear wheel spinning from rest to a final angular velocity of 250 rpm in 5.00 s.

$$250 \frac{rev}{min} \left(\frac{2\pi rad}{1 rev} \right) \left(\frac{1 min}{60 s} \right) = 26.2 \text{ rad/s}$$

A. Calculate the angular acceleration in rad/s^2 . Show your work.

$$\alpha = \frac{\Delta \omega}{\Delta t} = \frac{26.2 \text{ rad/s}}{5 s} = 5.24 \frac{rad}{s^2}$$

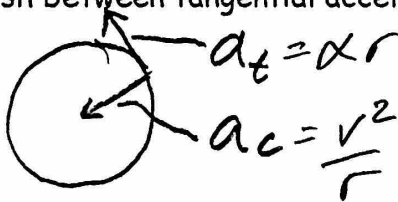
B. If she now slams on the brakes, causing an angular acceleration of -87.3 rad/s^2 , how long does it take the wheel to stop? Show your work.

$$\alpha = \frac{\Delta \omega}{\Delta t} \quad -87.3 \frac{rad}{s^2} = \frac{-26.2 \text{ rad/s}}{\Delta t} \Rightarrow \Delta t = 0.3 s$$

5. How are tangential acceleration and angular acceleration related?

"linear" accel. $\rightarrow a_t = \alpha r$

6. Distinguish between tangential acceleration (a_t) and centripetal acceleration (a_c)?



7. A powerful motorcycle can accelerate from 0 to 30.0 m/s (about 108 km/h) in 4.20 s. What is the angular acceleration of its 0.320-m-radius wheels? Show your work.

$$a_t = a = \frac{\Delta v}{\Delta t} = \frac{30 \text{ m/s}}{4.2 s} = 7.14 \text{ m/s}^2$$

$$a = \alpha r \Rightarrow 7.14 \text{ m/s}^2 = \alpha (0.32 \text{ m}) \frac{m}{rad}$$

$$\alpha = 22.3 \text{ rad/s}^2$$

ratio of m per radian