

Notes - 10.5 Angular Momentum and Its Conservation

1. Write the equation for linear momentum. $p = mv$

2. Write the equation for angular momentum. $L = I\omega$

3. State the Law of Conservation of Angular Momentum in words.

When net torque = 0, angular momentum remains constant

4. Write the equation for the Conservation of Momentum for.

$$L_i = L_f \quad I_i \omega_i = I_f \omega_f$$

6. Suppose an ice skater is spinning at 0.800 rev/s with her arms extended. She has a moment of inertia of $2.34 \text{ kg}\cdot\text{m}^2$ with her arms extended and a moment of inertia equal to $0.363 \text{ kg}\cdot\text{m}^2$ with her arms close to her body. (These moments of inertia are based on reasonable assumptions about a 60.0-kg skater.)

A. What is her initial angular velocity, in rad/s?

$$0.8 \frac{\text{rev}}{\text{sec}} \left(\frac{2\pi \text{ rad}}{1 \text{ rev}} \right) = 5.03 \text{ rad/s}$$

B. What is her initial angular momentum?

$$L_i = I_i \omega_i = (2.34 \text{ kg}\cdot\text{m}^2)(5.03 \text{ rad/s}) = 11.8 \frac{\text{kg}\cdot\text{m}^2}{\text{s}}$$

C. What is her final angular velocity?

$$L_i = L_f \quad 11.8 \frac{\text{kg}\cdot\text{m}^2}{\text{s}} = (0.363 \text{ kg}\cdot\text{m}^2)(\omega_f)$$

$$L_i = I_f \omega_f \quad \omega_f = 32.4 \text{ rad/s}$$

B. What is her rotational kinetic energy before and after she does this? Why does her KE_r change?

$$KE_{R \text{ before}} = \frac{1}{2} (2.34 \text{ kg}\cdot\text{m}^2) (5.03 \text{ rad/s})^2 = 29.6 \text{ J}$$

$$KE_{R \text{ after}} = \frac{1}{2} (0.363 \text{ kg}\cdot\text{m}^2) (32.4 \text{ rad/s})^2 = 191 \text{ J}$$

KE increases because she does work as she pulls in her arms.