

Newton's Laws in 2 Dimensions - Practice Problems #1

$\Sigma F = 0 = \Sigma F_x = \Sigma F_y$

1. The 10kg mass is in static equilibrium. Find the tensions in the two segments of rope.

$\Sigma F_x = 0 = T_{2x} - T_{1x} \Rightarrow T_{2x} = T_{1x}$

$\Sigma F_y = 0 = T_{1y} + T_{2y} - 98N$

$0.906T_2 = 0.643T_1$

$1.41T_2 = T_1$

$0 = 0.766T_1 + 0.423T_2 - 98N$

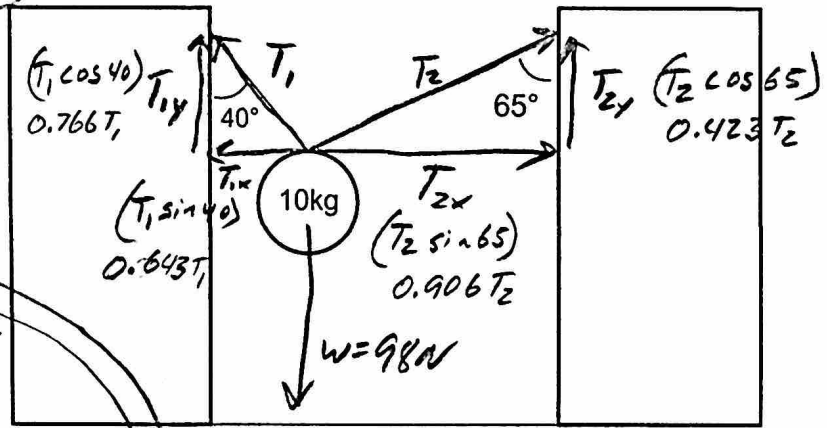
$0 = 0.766(1.41T_2) + 0.423T_2 - 98N$

$0 = 1.50T_2 - 98N$

$98N = 1.5T_2$

$T_2 = 65.2N$

$T_1 = 1.41(65.2N) = 91.9N = T_1$



2. Find the acceleration of the masses and the tension in the string.

$a = 0.61m/s^2$ CW

$T = 46N$

$\Sigma F_{11kg} = 49N - 37.8N - 4.5N = 6.7N$

$\Sigma F_{11kg} = 11kg(a)$

$11kg(a) = 6.7N$

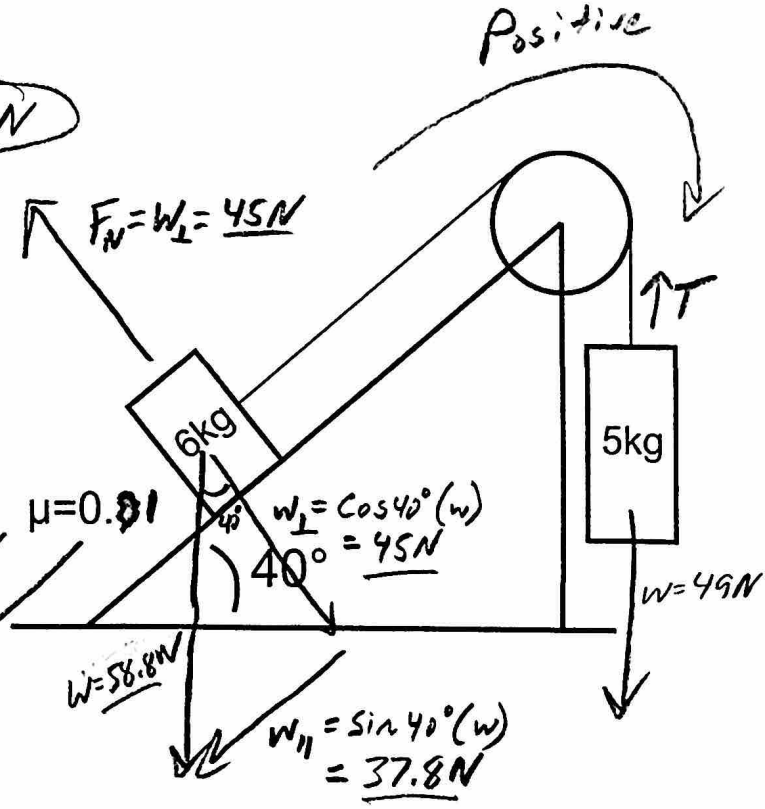
$a = 0.61m/s^2$ (clockwise)

$\Sigma F_{5kg} = T - 49N$

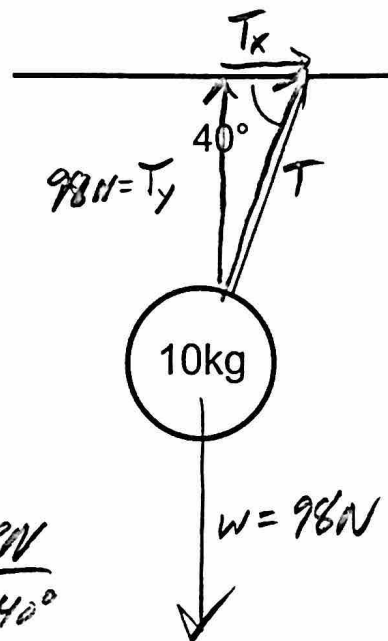
$\Sigma F_{5kg} = 5kg(-0.61m/s^2) = -3.05N$

$T - 49N = -3.05N$

$T = 46N$



3. The mass is suspended from the ceiling of a moving vehicle. The angle shown is constant. Find the acceleration of the mass and the tension in the string.



$$a = \underline{11.7 \text{ m/s}^2, \text{ rightward}}$$

$$T = \underline{152 \text{ N}}$$

$$\Sigma F_y = 0 = T_y - 98 \text{ N} \Rightarrow T_y = 98$$

$$\Sigma F_x = T_x \quad \tan 40^\circ = \frac{98 \text{ N}}{T_x} \Rightarrow T_x = \frac{98 \text{ N}}{\tan 40^\circ}$$

$$\Sigma F_x = 10 \text{ kg}(a)$$

$$10 \text{ kg}(a) = 117 \text{ N}$$

$$a = \underline{11.7 \text{ m/s}^2}$$

$$T_x = 117 \text{ N}$$

$$T = \sqrt{98^2 + 117^2}$$

$$T = \underline{152 \text{ N}}$$

4. Find the acceleration of the 8kg mass. ***To make this problem more interesting, use $\mu=0.2$, instead***

$$\Sigma F_y = 0 = F_N + 19.3 \text{ N} - 78.4 \text{ N} \Rightarrow F_N = 58.7 \text{ N}$$

$$\Sigma F_x = 11.8 \text{ N} - 23 \text{ N} = -11.2 \text{ N}$$

$$\Sigma F_x = 8 \text{ kg}(a)$$

$$8 \text{ kg}(a) = -11.2 \text{ N}$$

$$a = -1.4 \text{ m/s}^2$$

$$a = \underline{1.4 \text{ m/s}^2 \text{ leftward}}$$

