

Masses Hanging and Dragged at Angles – Newton's Laws in 2 Dimensions

Q2

The 10kg mass is in static equilibrium.
Find the tensions in the two segments of rope.

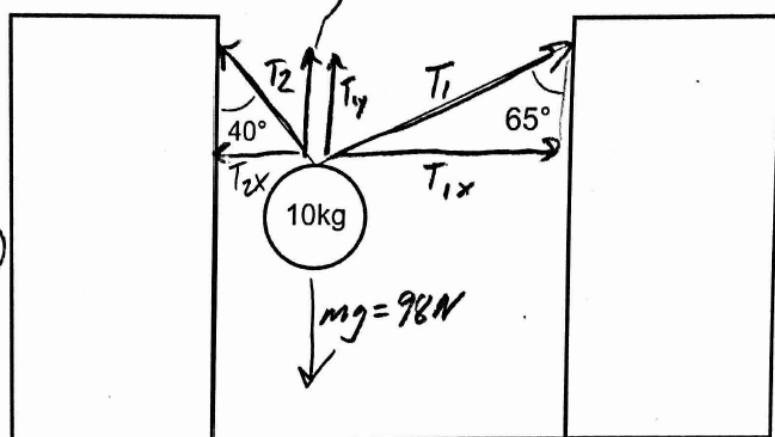
$$\sum F_y = 0 = T_{1y} + T_{2y} - 98N$$

$$\sum F_x = 0 = T_{1x} - T_{2x} \Rightarrow T_{1x} = T_{2x}$$

$$\sin 65^\circ(T_1) = \sin 40^\circ(T_2)$$

$$0.906 T_1 = 0.643 T_2$$

$$\underline{T_1 = 0.71 T_2}$$



$$0 = \cos 65^\circ T_1 + \cos 40^\circ T_2 - 98N$$

$$0 = 0.423 T_1 + 0.766 T_2 - 98N = 0.423(0.71 T_2) + 0.766 T_2 - 98N$$

$$0 = 0.766 T_2 + 0.3 T_2 - 98N$$

$$\underline{T_2 = 91.5N} \Rightarrow T_1 = 0.71 T_2 = 65N$$

1.

The 80kg mass is in static equilibrium. Find the tensions in the two segments of rope.

$$\sum F_x = 0 = T_{2x} - T_{1x} \Rightarrow T_{1x} = T_{2x}$$

$$\sum F_y = 0 = T_{1y} + T_{2y} - 784N$$

$$T_{1x} = \sin 70^\circ(T_1) \quad T_{2x} = \sin 50^\circ(T_2)$$

$$\begin{matrix} 0.94 \\ \uparrow \\ T_1 \end{matrix} \quad \begin{matrix} 0.766 \\ \uparrow \\ T_2 \end{matrix}$$

$$0.94 T_1 = 0.766 T_2$$

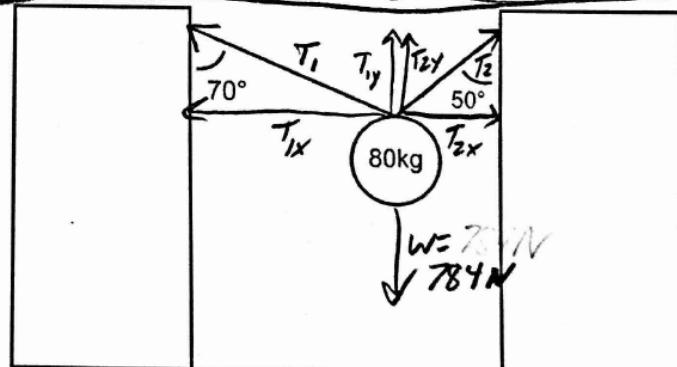
$$\underline{T_1 = 0.815 T_2}$$

$$\cos 70^\circ(T_1) + \cos 50^\circ(T_2) - 784N = 0$$

$$0.342(0.815 T_2) + 0.643(T_2) - 784N = 0$$

$$\cancel{0.279} T_2 + 0.643 T_2 = 784N$$

$$\underline{T_2 = 839N} \quad \begin{matrix} 850 \\ \downarrow \\ T_1 = 684N \end{matrix}$$



234

539

642

642

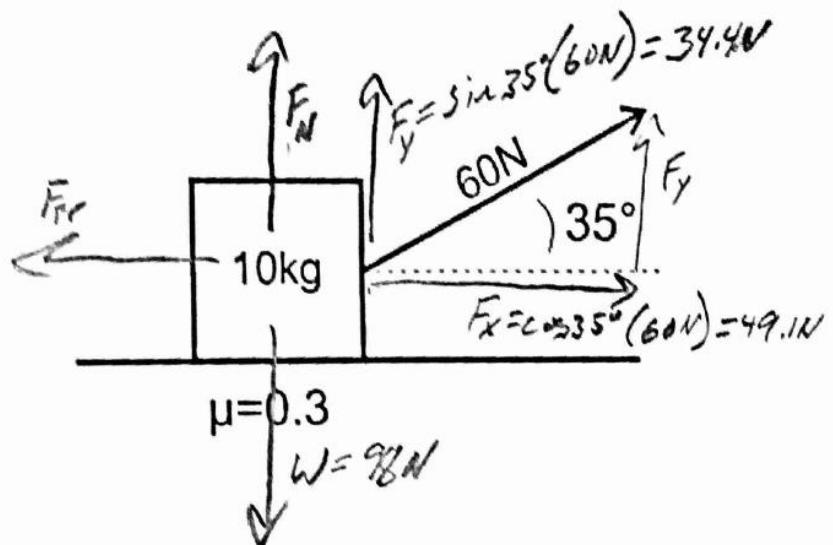
3. Find the acceleration of the 10 kg mass.

~~Diagram~~

$$\sum F_y = F_y + F_N - w = 0$$

$$0 = 34.4N + F_N - 98N$$

$$F_N = 63.6N$$



$$\sum F_x = F_x - F_f$$

$$= 49.1N - \mu F_N$$

$$= 49.1N - (0.3)(63.6N)$$

$$\sum F_x = 29.9N$$

$$\sum F_x = m a_x$$

$$29.9N = 10kg (a_x)$$

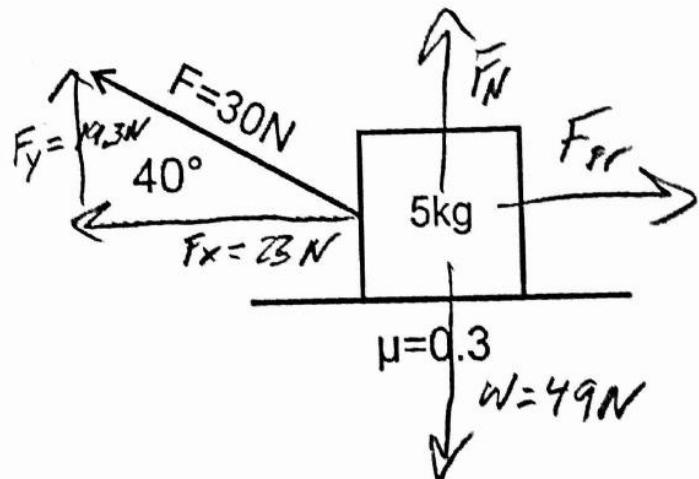
$$(a_x = 2.99 m/s^2)$$

4. Find the acceleration of the 8kg mass.

$$\sum F_y = F_y + F_N - w = 0$$

$$= 19.3N + F_N - 49N = 0$$

$$F_N = 29.7N$$



$$\sum F_x = F_f - F_x$$

$$= \mu F_N - F_x$$

$$= 0.3(29.7N) - 23N$$

$$= -14.1N$$

$$\sum F_x = m a_x$$

$$-14.1N = 8kg (a_x)$$

$$(a_x = -1.76 m/s^2)$$