

13

4.

Boat A has a mass of 10kg and a velocity of 3m/s. Boat B has a mass of 15kg and a velocity of -1m/s. The two boats collide and bounce away from one another. After the bounce, boat B has a velocity of 1.4m/s.

a. What is the velocity of boat A after the bounce?

$$-0.6 \text{ m/s}$$

b. What impulse is experienced by boat A during the collision?

$$F\Delta t = \Delta p = p_{\text{final}} - p_{\text{initial}} = (0.6 \text{ m/s})(10 \text{ kg}) - (10 \text{ kg})(3 \text{ m/s}) = -36 \text{ kg}\cdot\text{m/s}$$

c. What impact force is felt by boat B?

$$F(0.1 \text{ s}) = -36 \text{ kg}\cdot\text{m/s} \quad F = 360 \text{ N}$$

d. What impulse is experienced by boat B?

$$36 \text{ kg}\cdot\text{m/s}$$

e. What impact force is felt by boat A?

$$F = -360 \text{ N}$$

f. What is the coefficient of restitution for this collision?

$$e = \frac{v_B' - v_A'}{v_A - v_B} = \frac{1.4 \text{ m/s} - (-0.6 \text{ m/s})}{(3 \text{ m/s}) - (-1 \text{ m/s})} = \frac{2 \text{ m/s}}{4 \text{ m/s}} = 0.5$$

g. Is the collision elastic or inelastic?

$$e < 1$$

14. A softball of mass 0.220 kg that is moving with a speed of 8.5 m/s collides head-on and elastically with another ball initially at rest. Afterward the incoming softball bounces backward with a speed of 3.7 m/s. Calculate (a) the velocity of the target ball after the collision, and (b) the mass of the target ball.

Let A represent the moving softball, and let B represent the ball initially at rest. The initial direction of the softball is the positive direction. We have $v_A = 8.5 \text{ m/s}$, $v_B = 0$, and $v_A' = -3.7 \text{ m/s}$.

(a) Use Eq. 7-7 to obtain a relationship between the velocities.

$$v_A - v_B = -(v_A' - v_B') \rightarrow v_B' = v_A - v_B + v_A' = 8.5 \text{ m/s} - 0 - 3.7 \text{ m/s} = 4.8 \text{ m/s}$$

(b) Use momentum conservation to solve for the mass of the target ball.

$$m_A v_A + m_B v_B = m_A v_A' + m_B v_B' \rightarrow$$

$$m_B = m_A \frac{(v_A - v_A')}{(v_B' - v_B)} = (0.220 \text{ kg}) \frac{(8.5 \text{ m/s} - (-3.7 \text{ m/s}))}{4.8 \text{ m/s}} = 0.56 \text{ kg}$$